

What is a CIRCUIT?

↑ in the abstract, idealised sense

it is:

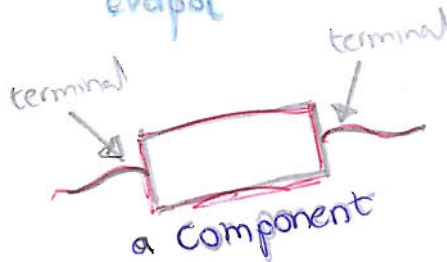
COMPONENTS

and

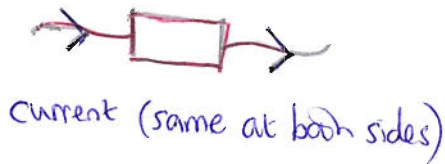
their

CONNECTIONS

- often "two-terminal" components



- We can define a current and voltage



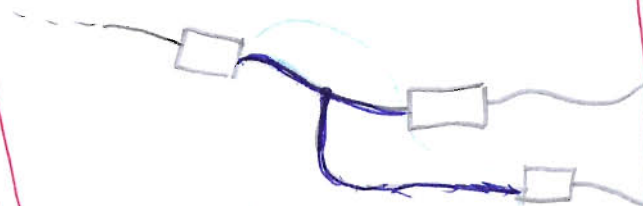
current (same at both sides)



difference in potential between sides

- several types: resistor, voltage source, etc.

- shown by "nodes" (ideal connections)



this is one node, joining three terminals

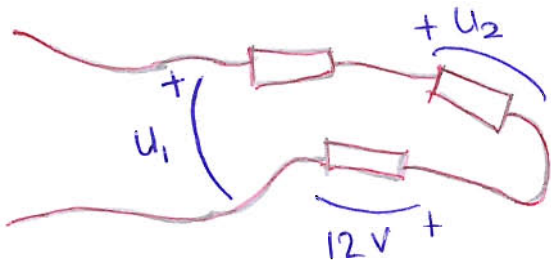
The node defines all the terminals it connects to as having the same potential, and as being able to exchange current.

The **components** determine one aspect of their current and voltage. (No component fully determines both of these.)

The **connections** provide further demands by Kirchhoff's laws.

→ **Together**, these two sets of "constraints" determine the solution for all voltages and currents in a circuit.

We often need to mark **voltages** across components, or more generally, between nodes:

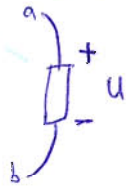


← Here are some voltages, marked with symbolic or number+unit quantities.

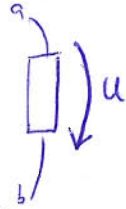
The '+' side shows that this side is greater in potential than the other side, by the marked amount.

(That might be a negative amount.)

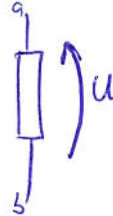
Other ways of showing voltage include:



common modern textbooks



common European way showing field direction or "current in resistor"

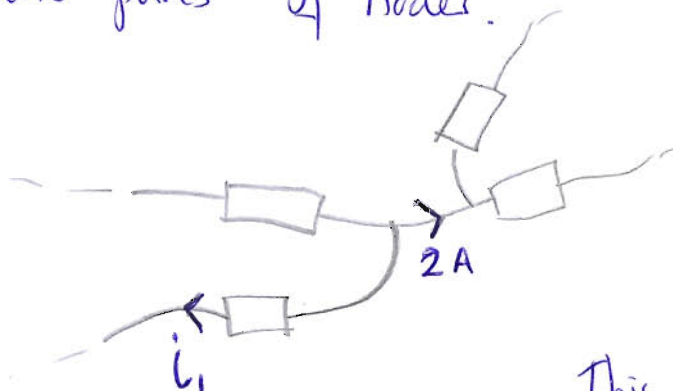


common English-language way showing change in potential from tail to head of arrow.

all mean the same thing.

I prefer the '+' or '+ -' method ... no doubt about meanings.

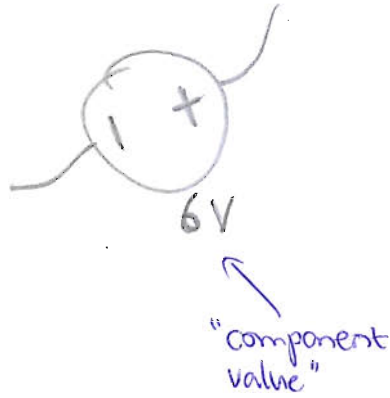
Likewise, we mark **currents** through components' terminals or other parts of nodes.



This is easy, using a little arrow.

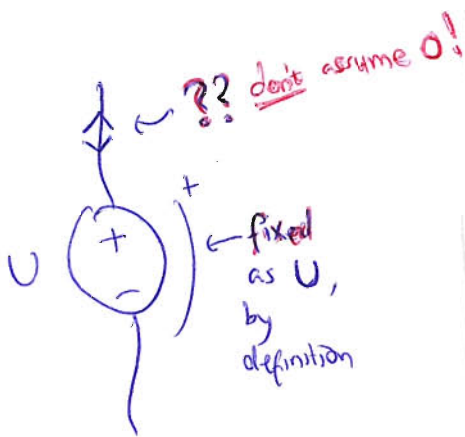
Define three core-components.

VOLTAGE SOURCE

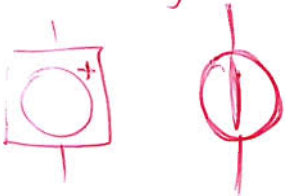


Difference of potential of '+' terminal compared to '-' terminal is fixed by the source's value (6V in this example).

The current is not at all determined by the source definition -- it is dependent on the rest of the circuit.



Other symbols include:

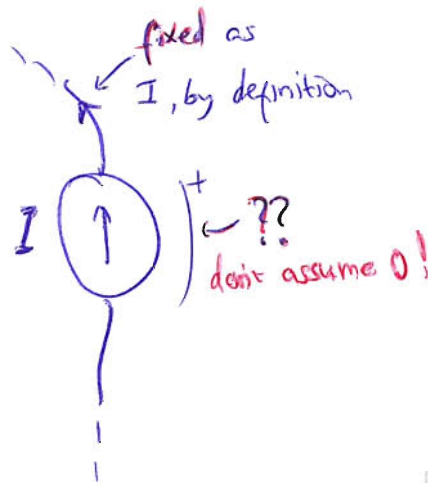


CURRENT SOURCE

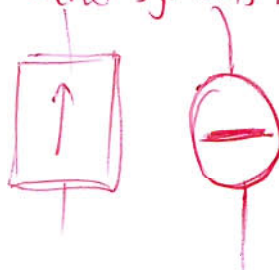


The current through the component is fixed by its value, (2A in this example).

The voltage depends on the rest of the circuit. The source will adjust to the voltage that is needed to cause the required current to flow.



Other symbols include:



RESISTOR



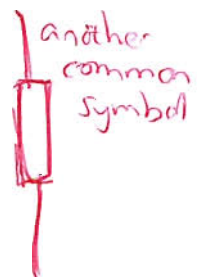
Voltage is not fixed by the component's definition.

Current is not fixed either!

But their **RATIO** (kvot) is fixed: Ohm's law:

$$R = \frac{U}{i}$$


The actual values depend on the rest of the circuit.



Note in most of this course material, the notation is that:

 is resistor

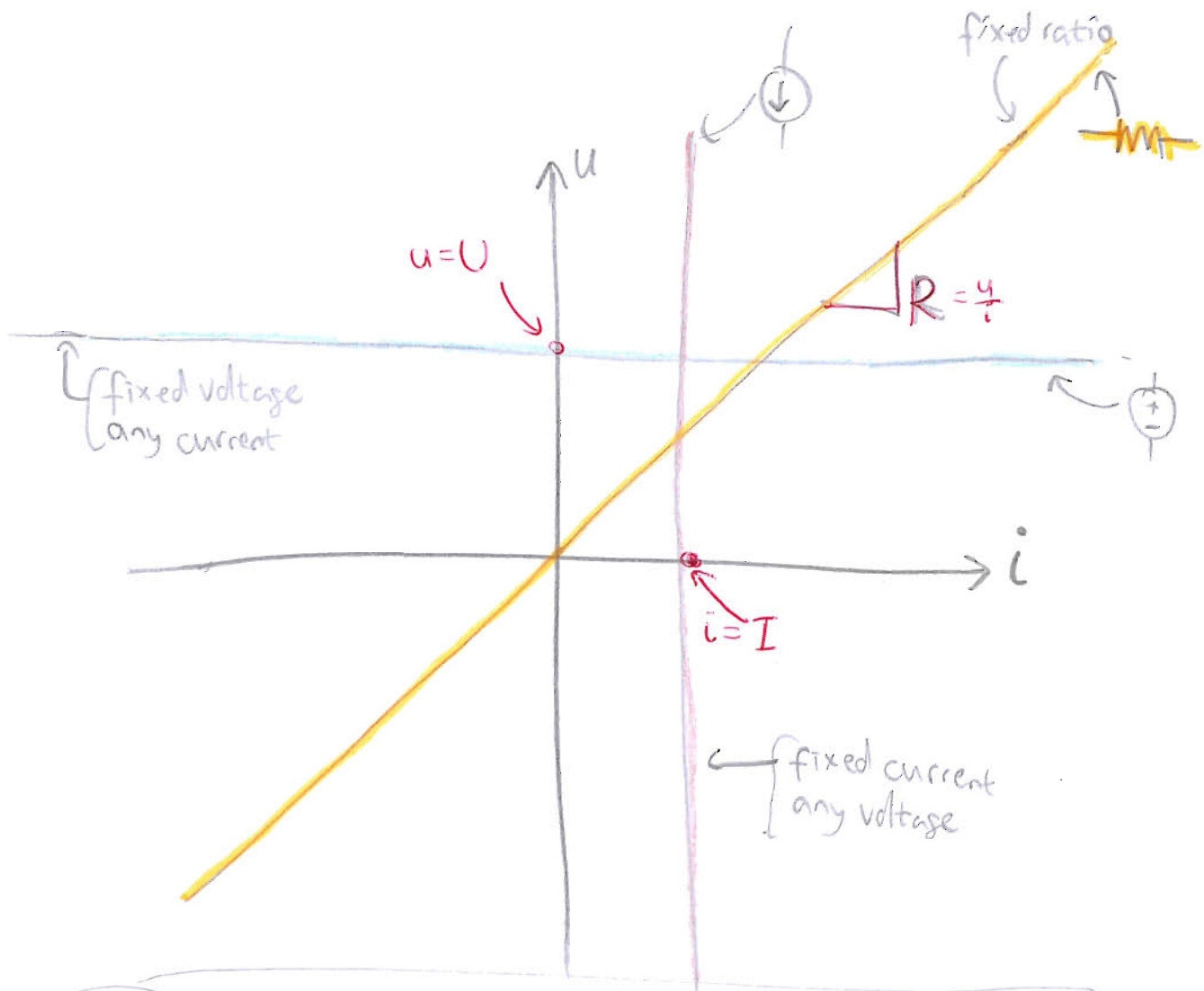
and

 is GENERIC COMPONENT with two terminals

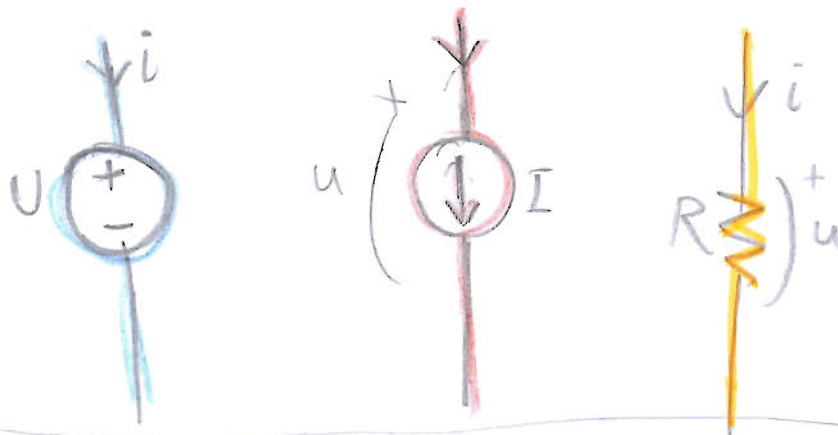
= could be voltage source, resistor, etc.

= So don't be surprised to see power being supplied by these symbols in later examples!

A graphical view of two-terminal components' u, i



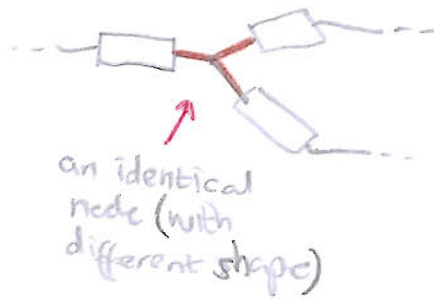
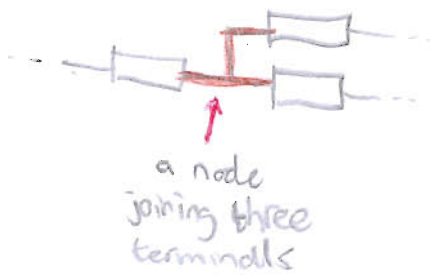
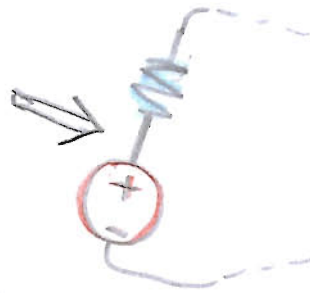
In the above, the definitions of u, i, U, I, R are:



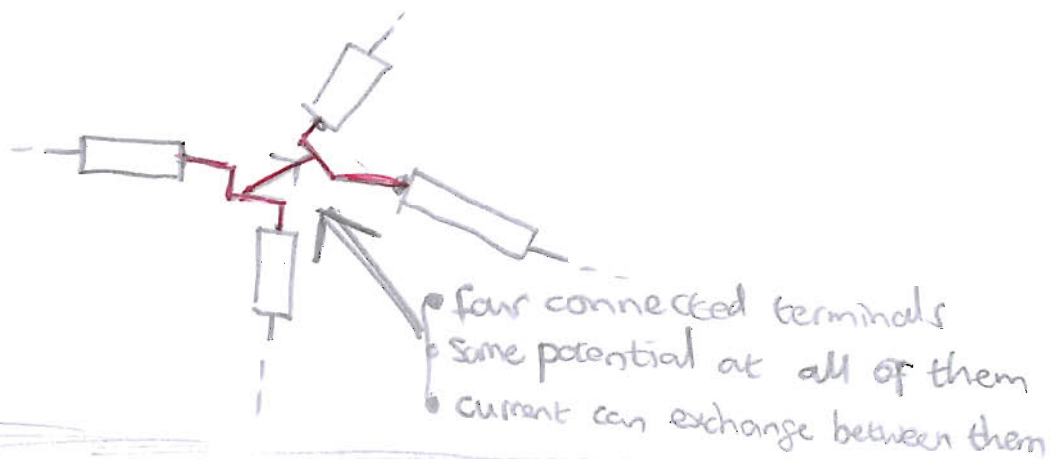
--- Some people like thinking of things as graphs. No problem if you don't — ignore it!

The CONNECTIONS: nodes

- Lines joining terminals show connections.
- all terminals linked in a group are one node.
- in circuit diagrams (ideal) the shape of the lines doesn't matter.



- a node defines all the connected terminals as having the same potential.
- a node shows that currents can flow between all the connected terminals.



In a simple lab circuit we think of "node \equiv wire" -
It is not necessarily a good assumption.

equivalent to

node \equiv wire
nod \equiv sladd

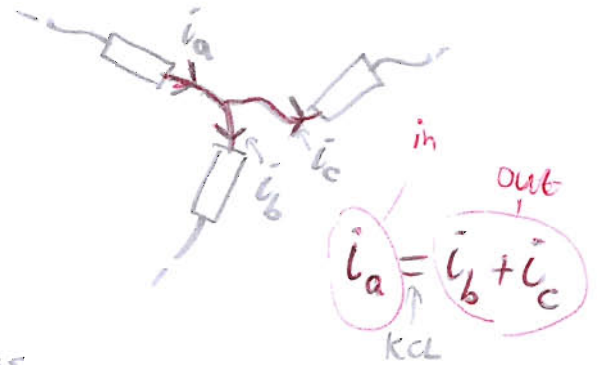
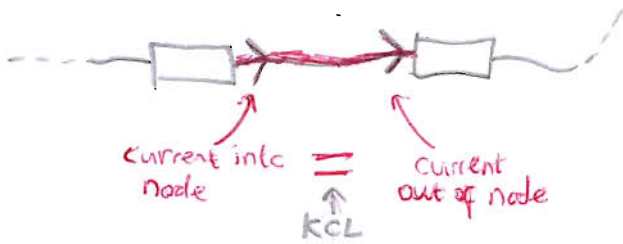
That is often ok when wires have resistance much less than the resistance of other components: es. $\ll 1\Omega$ wire, and $> 1k\Omega$ resistors.

In many other cases, wires are modelled as resistors (or inductors!) and nodes model their connection to other components.

Kirchhoff's CURRENT LAW (KCL)

"Current doesn't go missing in a circuit"

- classic example is to study one node for current-balance.

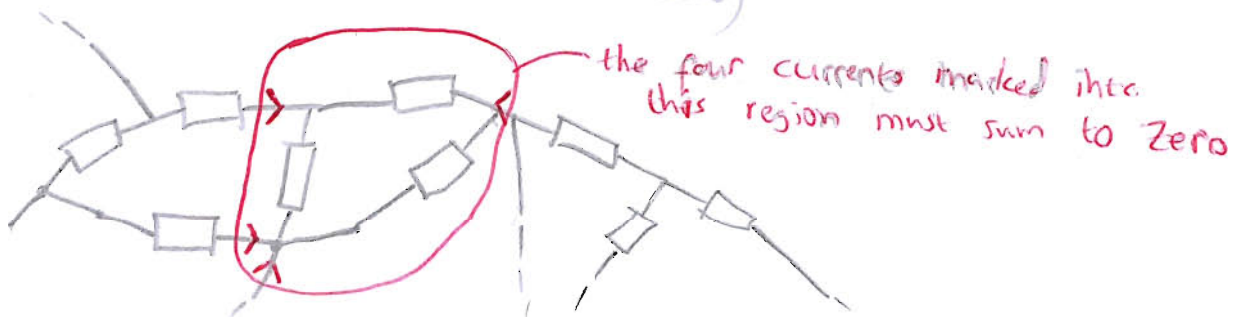


- the examples above state KCL as "what goes in equals what comes out"

- Sometimes it may be more systematic and reliable to avoid classifying connections by incoming versus outgoing arrows: "the currents defined into the node from each terminal must sum to zero"

- in the above example, this means $i_a - i_b - i_c = 0$, (which can be seen by rearranging the earlier equation)
- alternatively, change "into" to "out of": $-i_a + i_b + i_c = 0$

- KCL applies more generally, to currents into any region of a circuit (not just one node)



Kirchhoff's VOLTAGE LAW (KVL)

"the sum of voltages (potential changes) in a closed loop is zero"

or

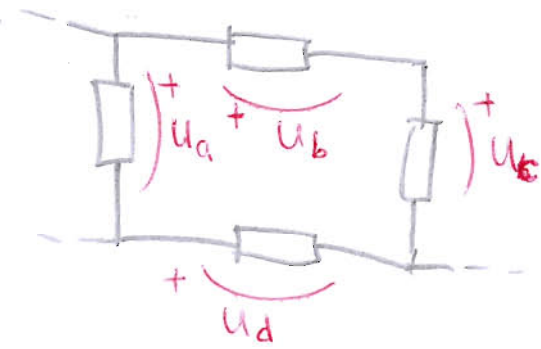
"circuit potential is conservative"

or

"a charge moving in a complete loop in a circuit loses as much energy as it gains"

↑
proportional to voltage for a given charge

to apply this we could equate gains to losses



if we choose to go clockwise from bottom left, we gain U_a then lose U_b then lose U_c then gain U_d

$$\underbrace{U_a + U_d}_{\text{gained potential}} \stackrel{\text{KVL}}{=} \underbrace{U_b + U_c}_{\text{lost potential}}$$

or we can just sum the total gains (with losses seen as negative gains) and equate to zero:

$$U_a - U_b - U_c + U_d = 0$$

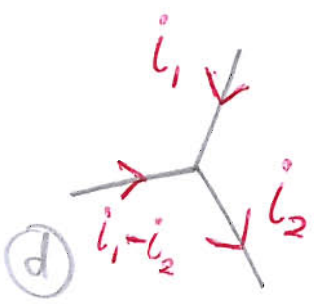
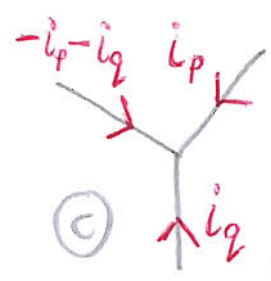
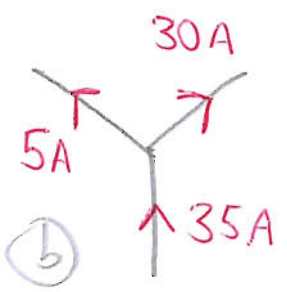
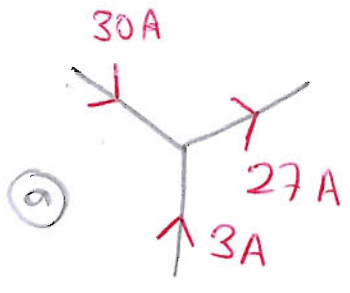
↑
KVL

- it's the same result, rearranged
- another rearrangement is obtained by going anticlockwise (motors)

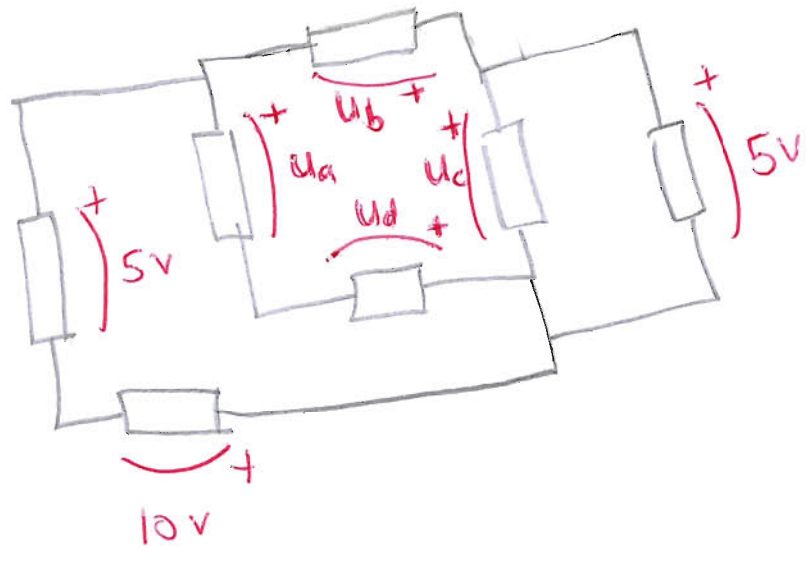
⇒ lots of ways to write KCL & KVL.
need to be very CAREFUL and SYSTEMATIC to avoid errors.

Quiz

Which of the following is/are WRONG (by KCL)?



Which of the following is/are WRONG (by KVL)?



- (a) $u_a + u_b - u_c + u_d = 0$
- (b) $u_b = 0$
- (c) $u_c = 5V$
- (d) $u_d - u_a = 5V$

(Solutions on next page)

Solutions

KCL

- (a) WRONG: 33 A goes in but 27 A comes out
- (b) right: 35 A in, 35 A out
- (c) right: total current going in is $\underbrace{-i_p - i_q + i_p + i_q}_{=0 \text{ (balances)}}$
- (d) WRONG: total going in is $\underbrace{i_1 + (i_1 - i_2) + (-i_2)}_{=2(i_1 + i_2)}$
not necessarily zero.

KVL

- (a) WRONG: needed " $-u_d$ " instead of " $+u_d$ "
- (b) WRONG: KVL in the loop of u_b and all the components with numeric values, gives:
 $5V + u_b - 5V - 10V = 0 \Rightarrow u_b = 10V$
- (c) WRONG: KVL in the loop of the two rightmost resistors gives
 $u_c - 5V = 0 \Rightarrow u_c = 5V$
- (d) right: KVL in the leftmost loop gives:
 $5V - u_a + u_d - 10V = 0$
 $\Rightarrow u_d - u_a = 5V$

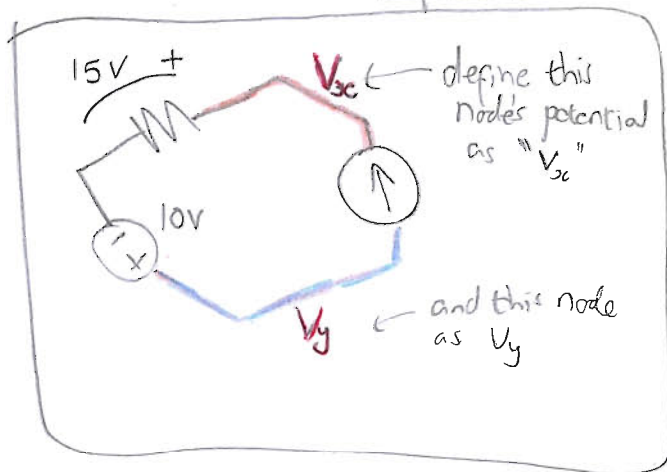
Potential

same thing --

We've mentioned **voltages**
(e.g. across components)

and **"changes of potential"**
(e.g. in KVL)

Potentials can be defined:



by looking at the marked voltages we can see that

$$V_y - 10V + 15V = V_{zc}$$

there's a nice Swedish term for this process of following changes of potential: **"potentialvandring"**

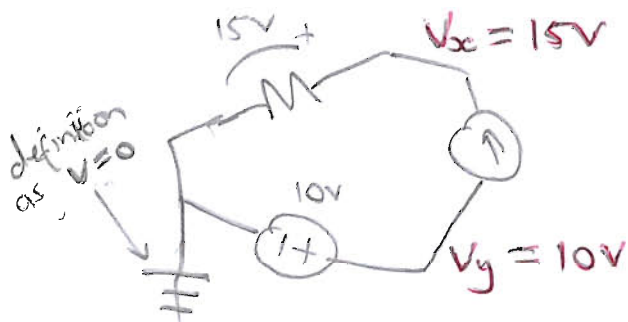
hence $V_{zc} - V_y = 5V$

But the circuit's voltages only let us find $V_{zc} - V_y$ --- what **is** V_{zc} ?
(a voltage) (or V_y)

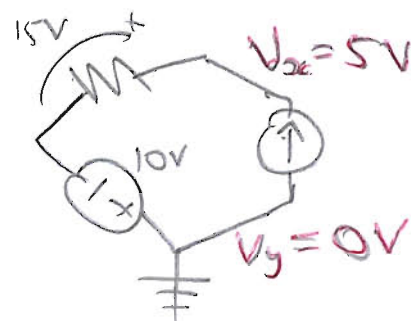
We have to define a value of one of the potentials in a circuit, if we want potentials to have defined values.

One option would be to say e.g. "let $V_{zc} = 20V$ ".
(Then in our case, $V_y = 15V$).

Another is to mark a node as zero potential (reference, earth, ground) (jord)

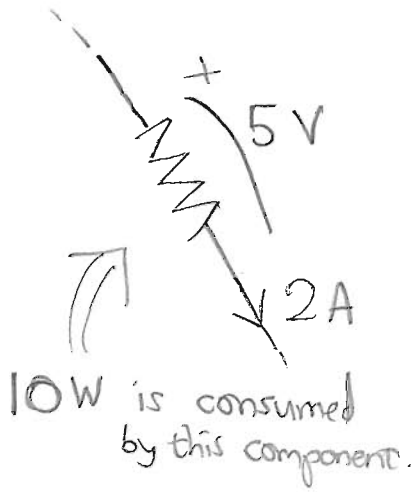


or



or ----

Power calculations

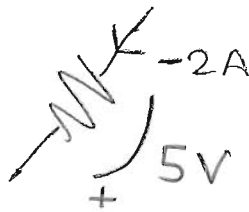
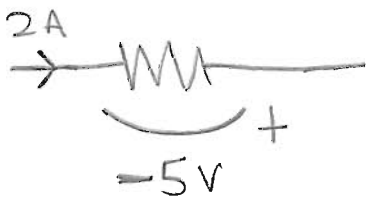


Here, "2 coulombs of charge every second lose 5 joules each."

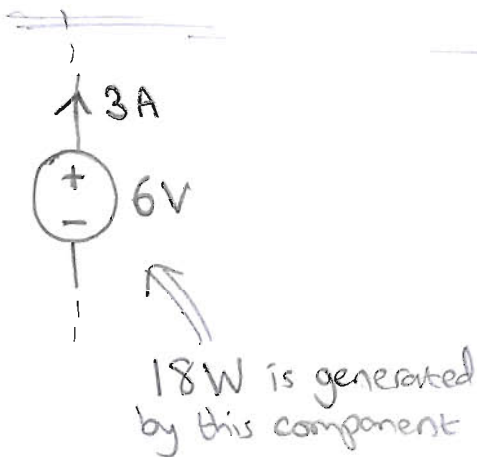
The power that this component takes from the circuit is therefore 10W.

$$[V] = \frac{[J]}{[C]} \quad [W] = \frac{[J]}{[s]} \quad [A] = \frac{[C]}{[s]}$$

The same is true in these cases:



Negative voltage or current means that the actual direction is opposite to the marking:

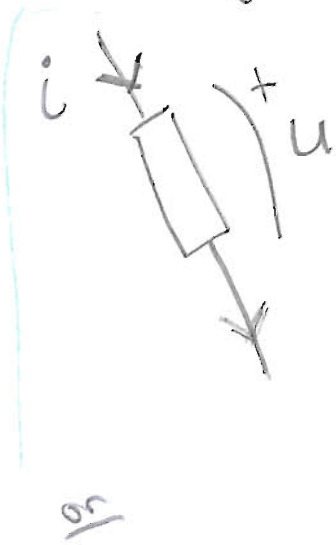
$$\begin{matrix} \uparrow 5V \equiv \downarrow -5V \\ \uparrow \\ \text{equivalent} \end{matrix} \quad \text{and} \quad \downarrow 2A \equiv \uparrow -2A$$


In this case, the charge is given energy when it passes through the component.

The component supplies 18W to the circuit. (förserjor)

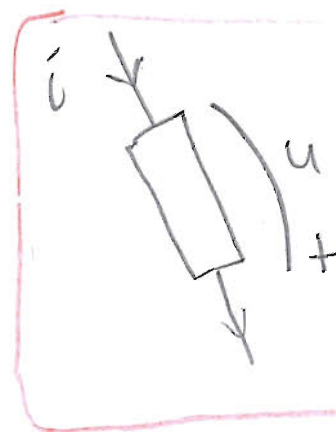
power(2)

More generally, with symbolic quantities:



current i goes down in potential by u


the power {
 supplied to component
 consumed by component
 delivered to component
 taken from rest of circuit
 etc. } = ui



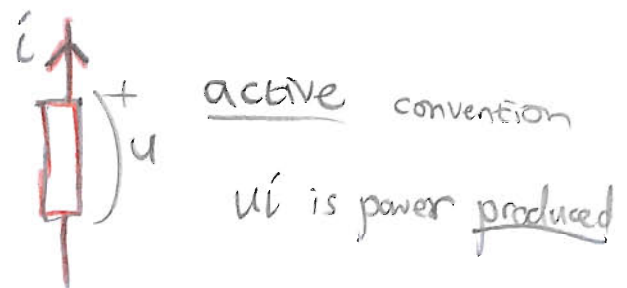
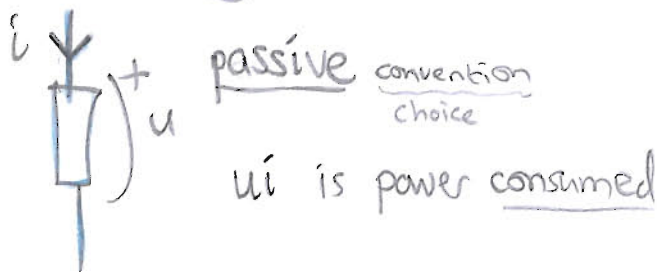
current i goes up in potential by u

the power {
 supplied from
 generated by
 produced by } the component = ui

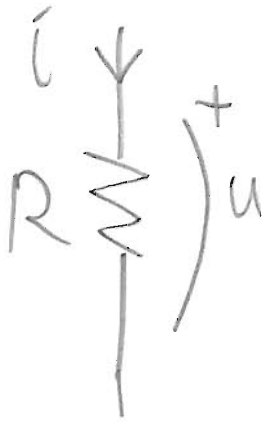
So, depending on the relative direction of the marked u and i , the product $P = ui$ can give either the power consumed by or the power produced by the component.

If we want the opposite, we negate it:  $P_{\text{produced}} = ui$
 $P_{\text{consumed}} = -ui$

There are names for the two possible "relative directions" for marking u and i :



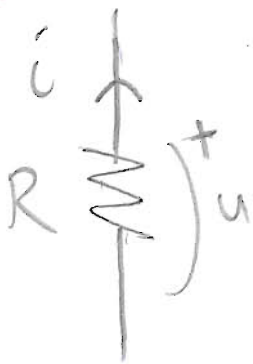
For Ohm's law too, the relative directions are important.



here the current is marked going down in potential by an amount u :

$$R = \frac{u}{i} \quad (\text{Ohm's law, with } u \text{ \& } i \text{ following the passive convention})$$

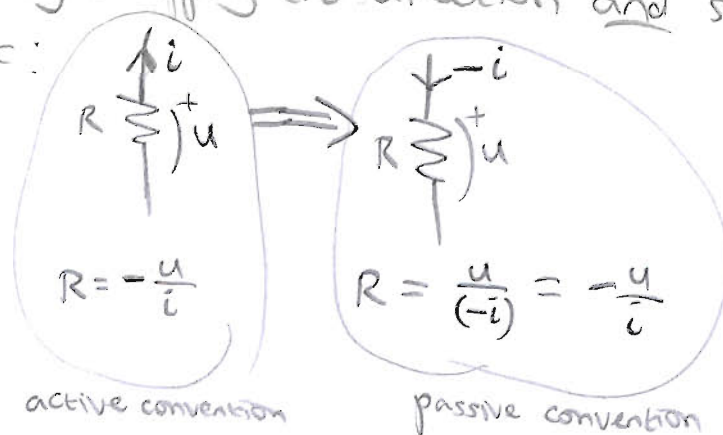
for a resistor, the current is pushed down the potential gradient



but here, the marked current is being pushed up in potential by an amount u ;

$$R = -\frac{u}{i} \quad (\text{Ohm's law, with } u \text{ \& } i \text{ following the active convention})$$

One way to see this is to make the second case look like the first by swapping the direction and sign of voltage or current:

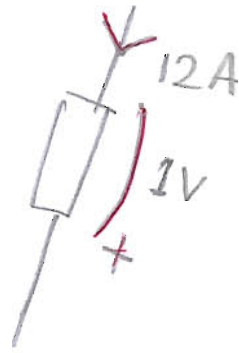


Quiz

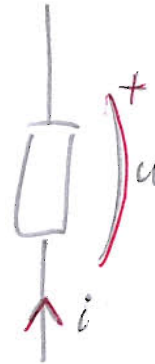
a



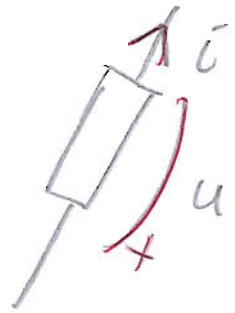
b



c



d



$$\text{Let } \begin{cases} u = 5V \\ \bar{i} = -3A \end{cases}$$

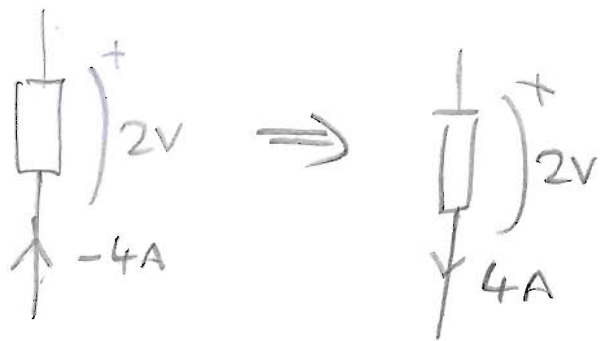
- ① Which component produces the most power?
- ② How much does each consume?

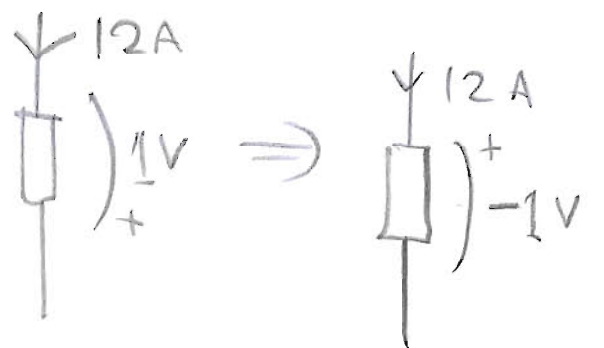
SOLUTION

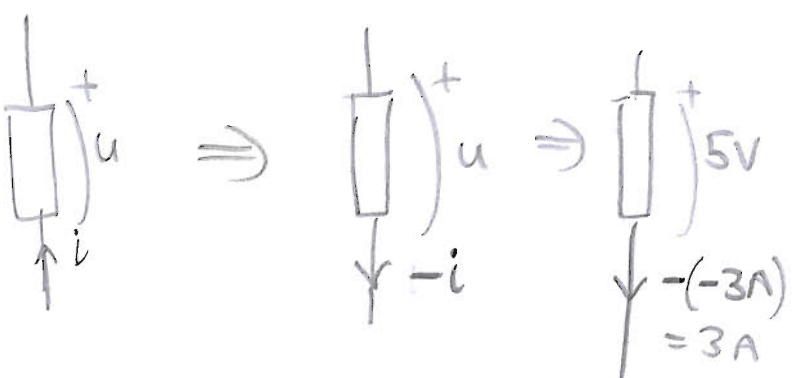
① The component 'd' produces most power — see below.

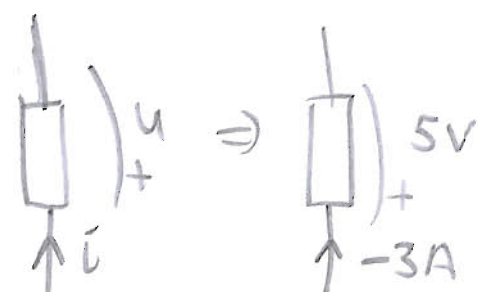
② Lets find how much each consumes.

We can rewrite in passive convention by swapping direction and sign if its in active convention.

⑤  $\Rightarrow 2V \cdot 4A = 8W$
consumed

⑥  $\Rightarrow (-1V) \cdot 12A = -12W$
consumed

⑦  $\Rightarrow 5V \cdot 3A = 15W$
consumed

⑧  $\Rightarrow 5V \cdot (-3A) = -15W$
consumed

already passive convention

Dependent sources

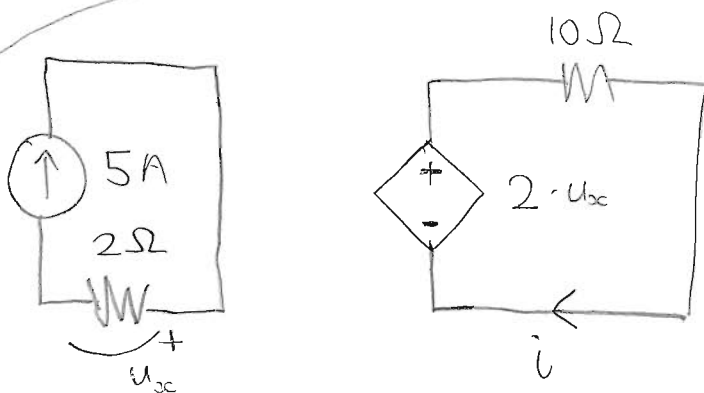
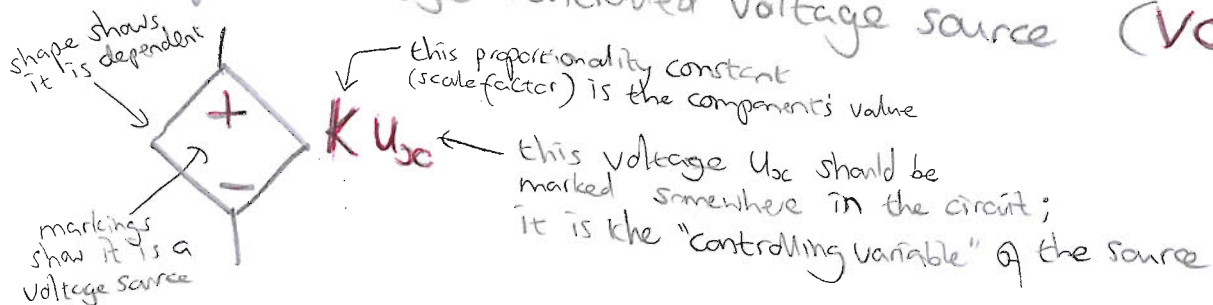
We have seen INDEPENDENT sources: U  I 

Their component-values (eg. U and I) don't depend on anything else in the circuit.

DEPENDENT SOURCES are different in that their output is proportional to a voltage or current defined somewhere in the circuit!

Their component-value is the proportionality constant. We use a diamond shape to show a dependent source.

Example: voltage controlled voltage source (VCVS)



find i

In this case the VCVS behaves as a voltage source of $2 \cdot U_{bc}$.

We see the marked definition of U_{bc} , which by KVL + Ohm tells us

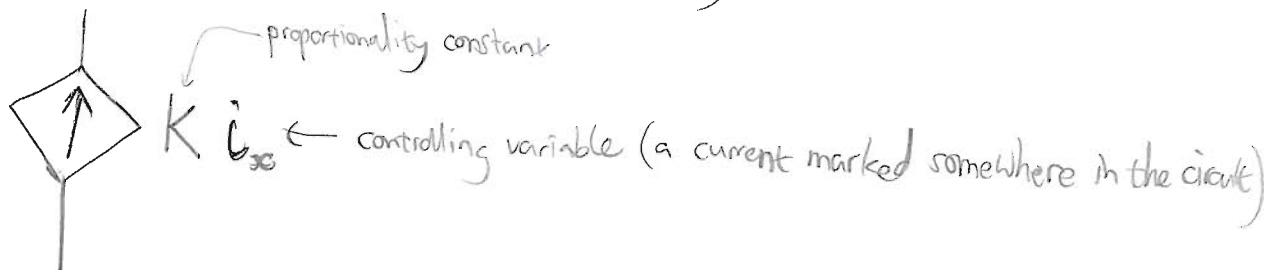
$$U_{bc} = 5A \cdot 2\Omega = 10V$$

Therefore,

$$i = \frac{2 \cdot 10V}{10\Omega} = 2A$$

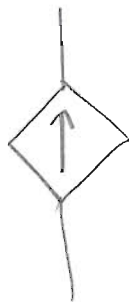
There are 4 dependent sources.
We've seen the VCVS:

The current controlled current source (CCCS) is:



The others can be guessed:

VCCS



the component's value
this could be called K again, but it is a $\frac{\text{current}}{\text{voltage}}$ ratio
so sometimes we choose another letter to show
it is not dimensionless.

$G \cdot U_x$ ← controlling variable ... could be called U_x or U_1 or U_2 ...

CCVS



ratio $\frac{\text{voltage}}{\text{current}}$

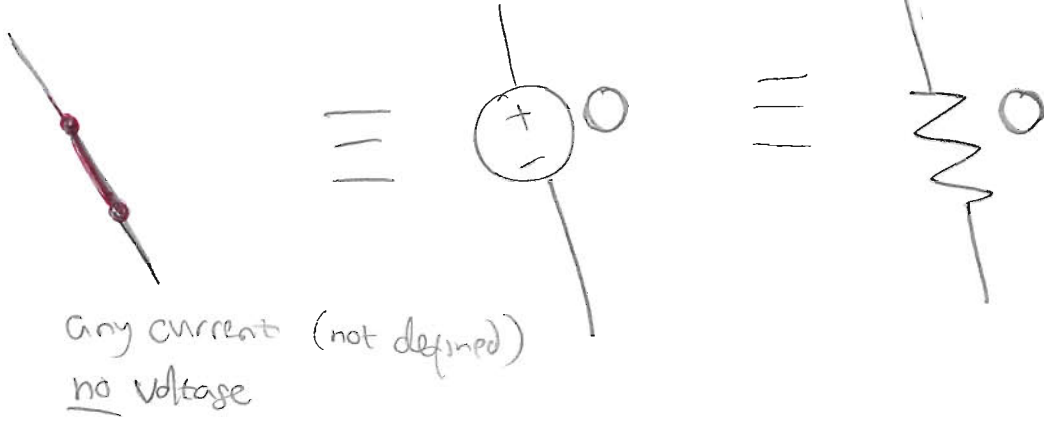
$H \cdot i$ ← controlling variable

Strange things (dependent sources)?

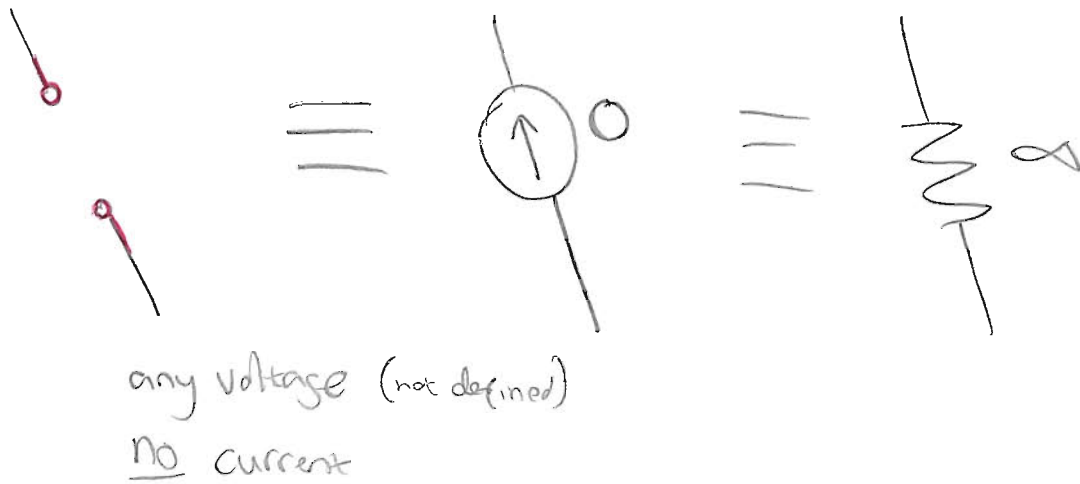
They're used a lot to make models of transistors and electronic circuits — useful in later courses.

Other components/concepts

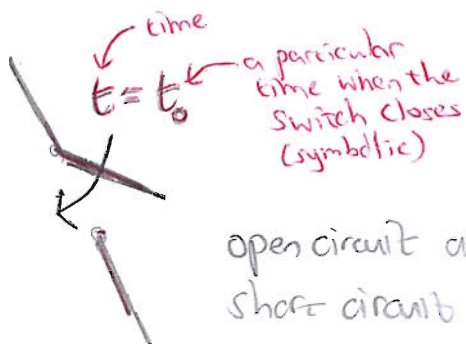
short circuit



open circuit

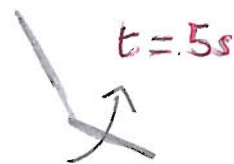


Switch with time



open circuit at $t < t_0$
 short circuit at $t \geq t_0$

closing switch

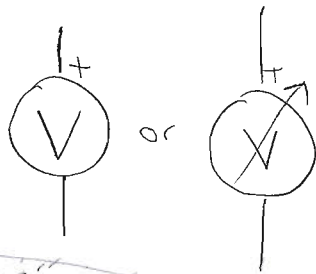


short circuit at $t < 5s$
 open circuit at $t \geq 5s$

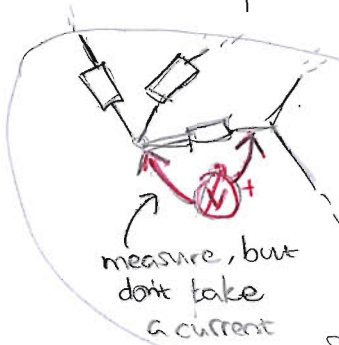
opening switch

Meters for measuring circuit quantities.

VOLTMETER

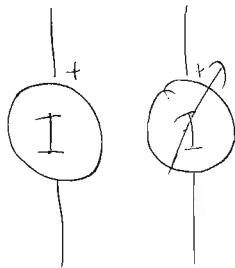


- show the voltage of its '+' terminal relative to the other
- should look like open circuit in how the circuit 'sees' it

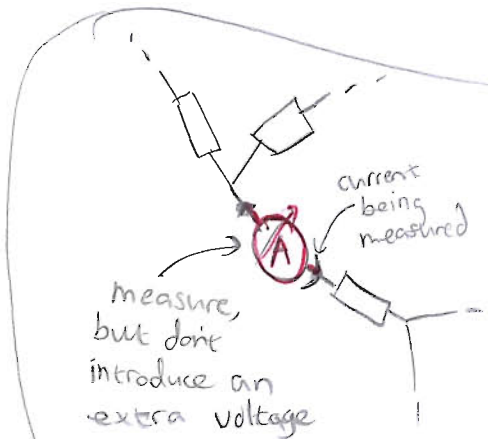


To measure a voltage, the meter is connected between two potentials, i.e. two nodes. If the meter does not behave like open circuit, some current may flow between the nodes --- so we have changed the circuit --- not good.

AMMETER



- show the current passing through from '+' terminal to the other.
- should look like short circuit



To measure a current, the circuit is broken and the ammeter is inserted to join the break - the current flows through it.

If it does not behave as a short circuit, some voltage can exist across the meter.

Then were measuring on a different circuit from the one we were trying to measure! The result could be unacceptably wrong.

Real meters are not ideal, but should be chosen "good enough"

$$\text{voltmeter } R_{\text{meter}} \neq \infty \xleftarrow{\text{ideal}} \text{ but } R_{\text{meter}} \gg R_{\text{circuit}}$$

$$\text{ammeter } R_{\text{meter}} \neq 0 \xleftarrow{\text{ideal}} \text{ but } R_{\text{meter}} \ll R_{\text{circuit}}$$

Other meters --- just for background knowledge

ohm meter

measure resistance by making a current or a voltage, measuring the other quantity, then dividing $\frac{V}{I} = R$

Common in labs

multimeter

combines a { voltmeter
ammeter
ohmmeter

widely used

power meter

measure voltage and current: multiply them

energy meter

integrate power over time

like the electricity meter in a home: kWh
(kilowatt hour)

Charge meter
or electrometer

useful in some laboratories: mainly "electrostatics"